



Local Galaxies

Fundamental relations for Ellipticals & dEs :

Color – magnitude relation : brighter Es are redder

Luminosity – metallicity relation : brighter Es are more metal-rich

Faber – Jackson relation : central velocity dispersion increases with luminosity

→ distance / mass determination

Kormendy's relations :

brighter Es have large effective radii

brighter Es have lower (average) surface brightness

Sphs (and GCs) do not follow Kormendy's relations

Fundamental Plane relations : effective radius – surface brightness – luminosity – central velocity dispersion

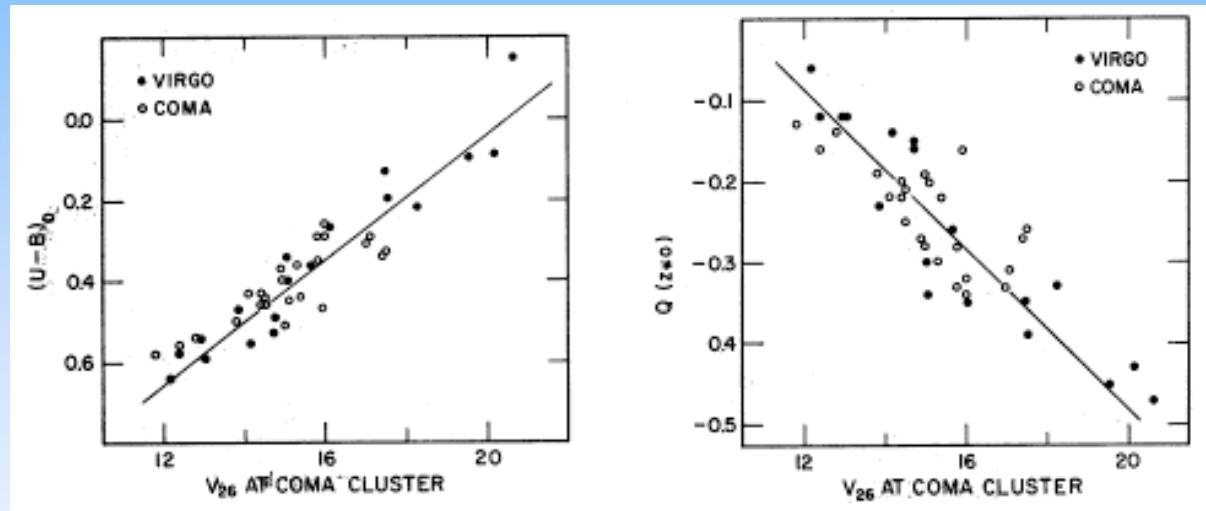
M/L increases with L

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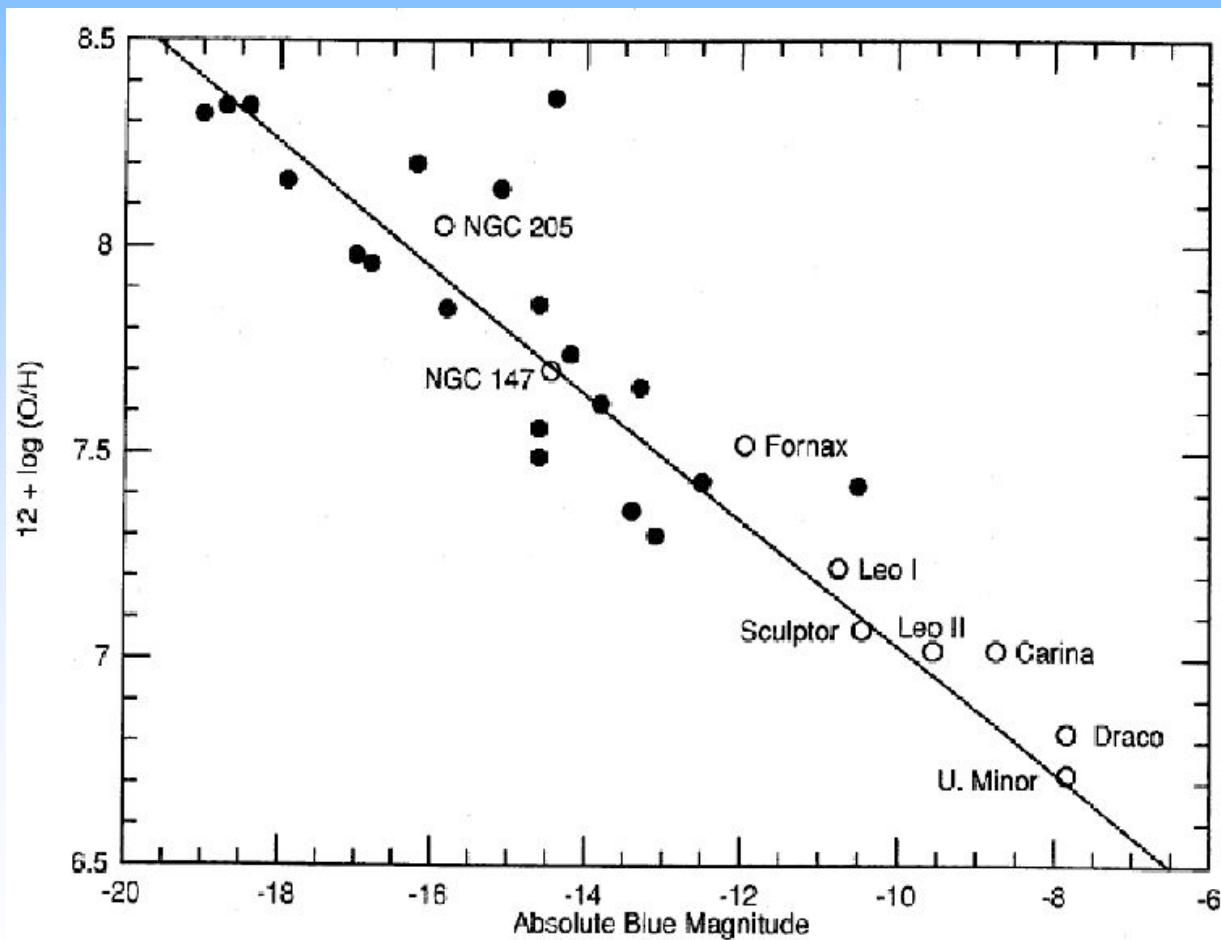
(de Vaucouleurs 61, 72, fffff)



Local Galaxies

Fundamental relations for Ellipticals & dEs :

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Vader 86,
Bica & Alloin 87,
Skillman 89



Local Galaxies

Fundamental relations for Ellipticals & dEs :

Faber – Jackson relation : central velocity dispersion increases with luminosity

(Faber & Jackson 76)

→ distance / mass determination

$$L_v \sim \sigma^\epsilon, \quad \sigma: \text{central velo. disp.}$$

$$M_r \sim \sigma^4 / (\rho_r r) \rightarrow M/L \text{ increases with } L$$

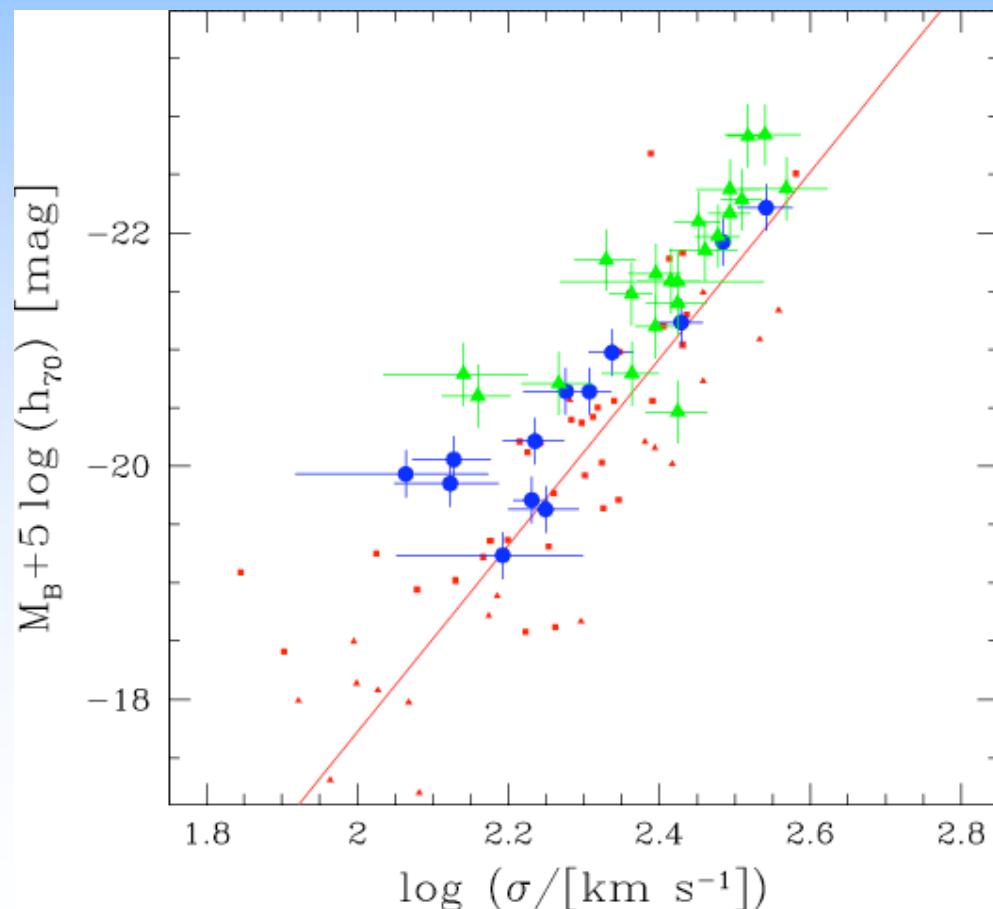
$\epsilon \sim 4$ for bright gals
 $\epsilon \sim 3.2$ for faint gals
 $\epsilon \sim 5.4$ for cD gals

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Faber – Jackson relation : central velocity dispersion increases with luminosity

(Faber & Jackson 76)



(Ziegler+05)

Local Galaxies

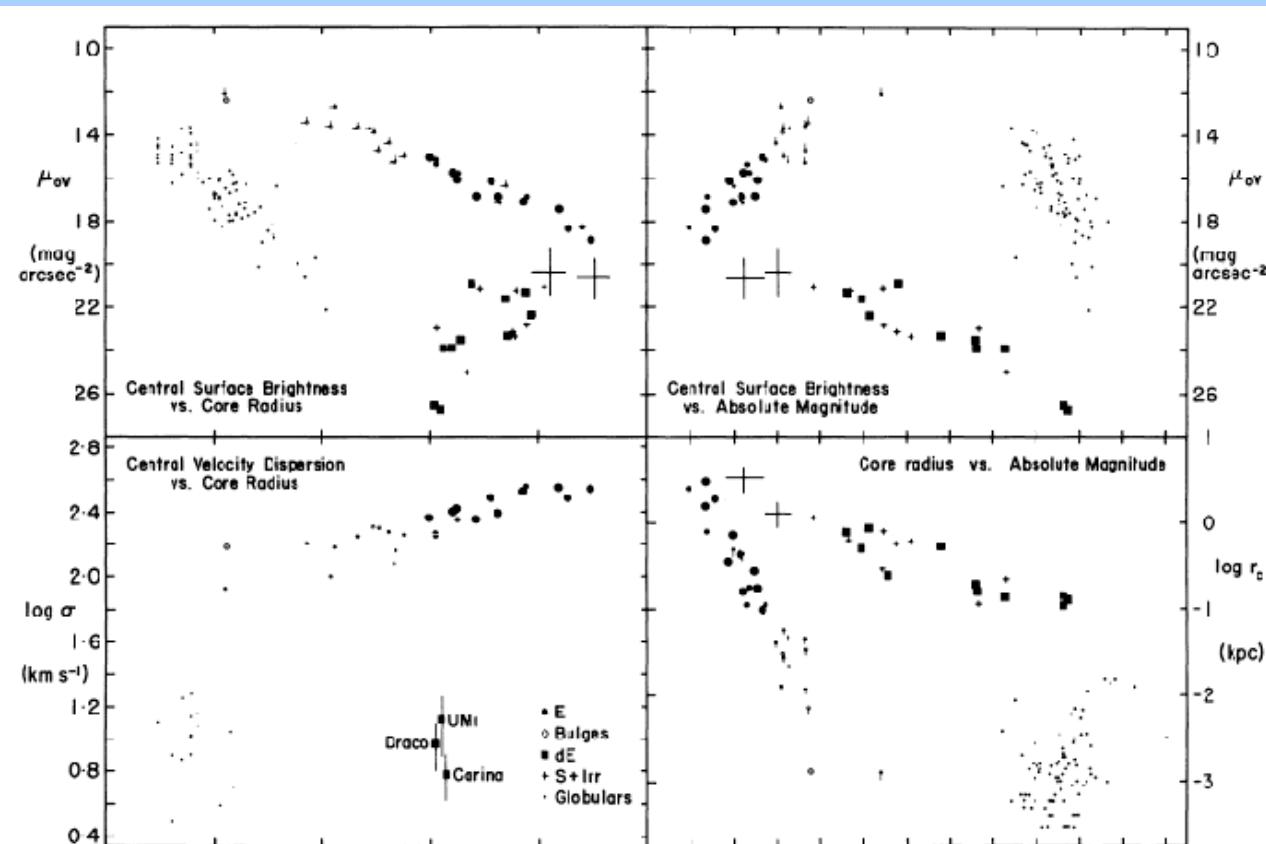
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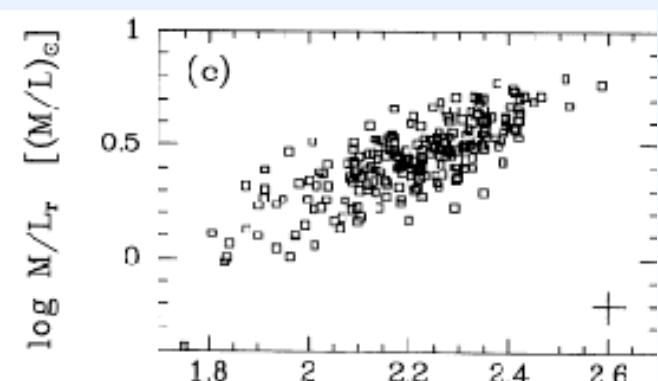
Fundamental relations for Ellipticals & dEs :

Fundamental Plane relations : effective radius – surface brightness – luminosity – central velocity dispersion

3 global parameters enough to describe structure of normal ellipticals, 2-dimensionally correlated: plane

$$L_v \sim \sigma_e^a I_e^b \quad r_e \sim \sigma_e^c I_e^d$$

	a	b	c	d
Dressler+87	2.65	-0.65	1.33	-0.83
Djorgovski & Davis 87	3.45	-0.86	1.39	-0.90

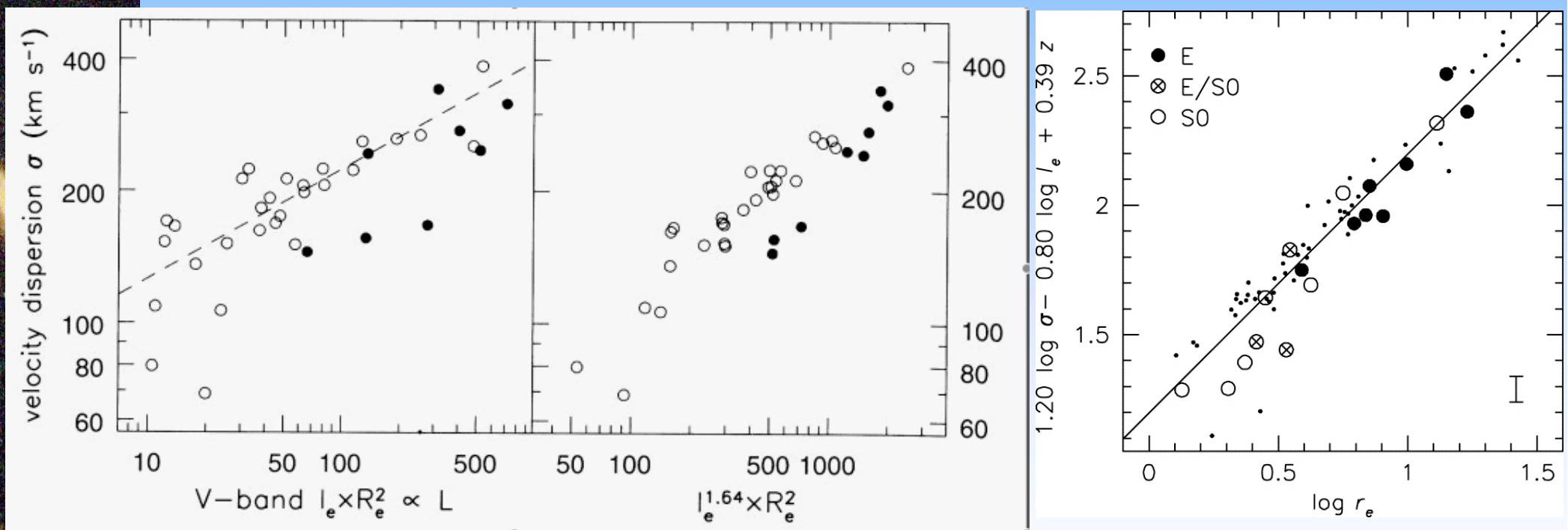


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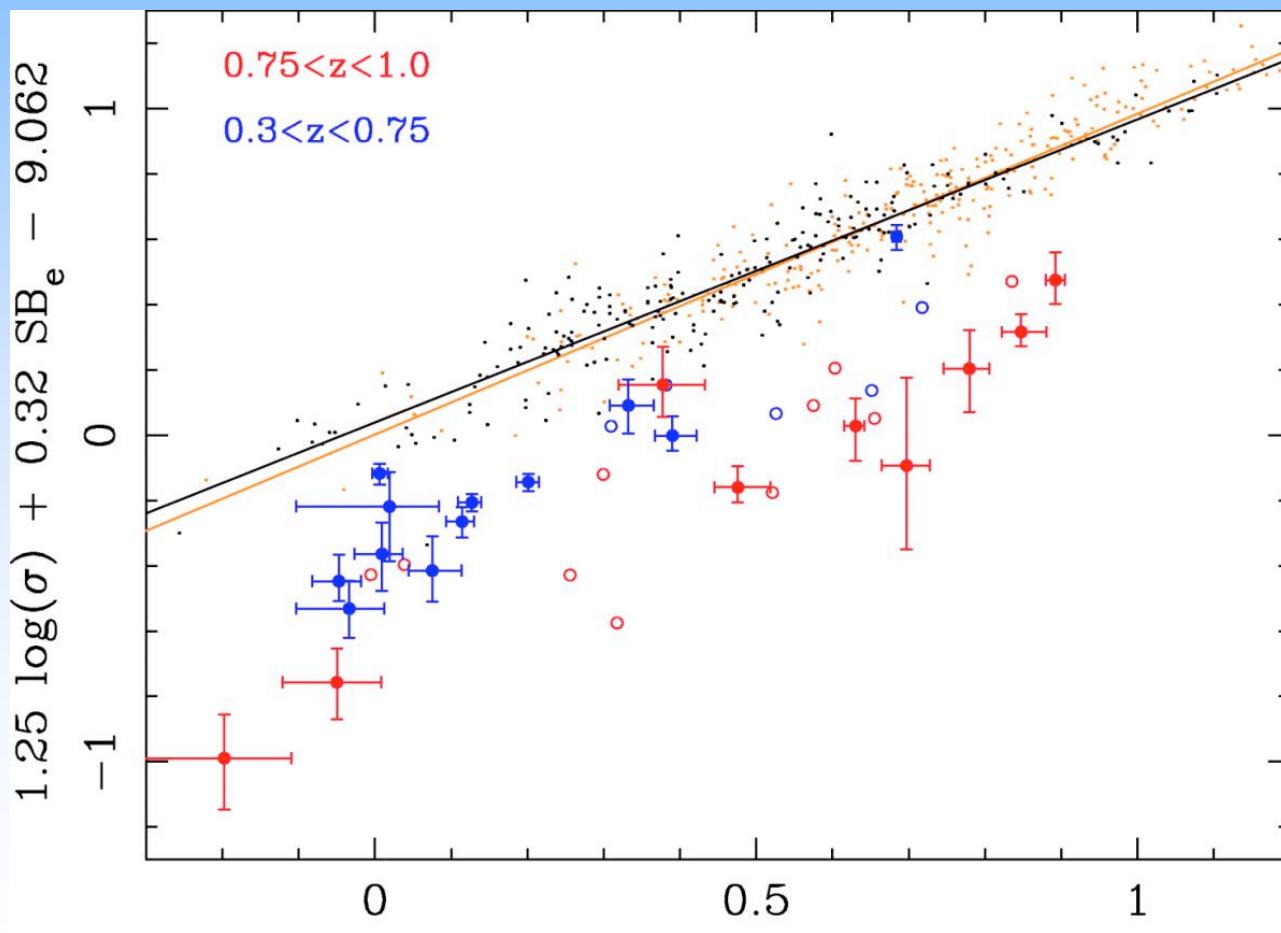


Local Galaxies

Fundamental relations for Ellipticals & dEs :

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M/L increases with L



Redshift evolution



Local Galaxies

Fundamental relations for Spirals :

Luminosity – metallicity relation : for spirals and Irrs:
brighter Sps/Irrs have higher ISM metallicities

Tully – Fisher relation : brighter Sps have higher max.
rotation velocities

→ distance / mass determination

rotational velocity $\sim M(DM)$

better correlation with NIR than with optical luminosities

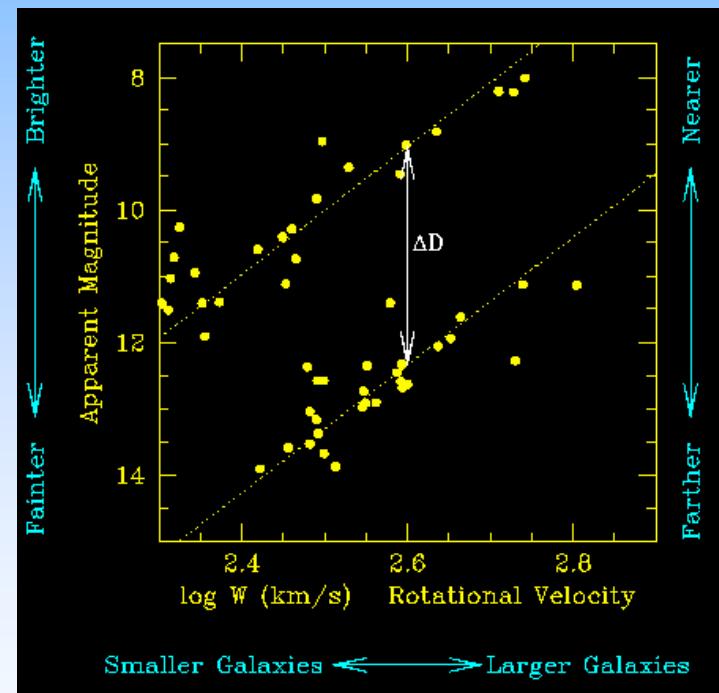
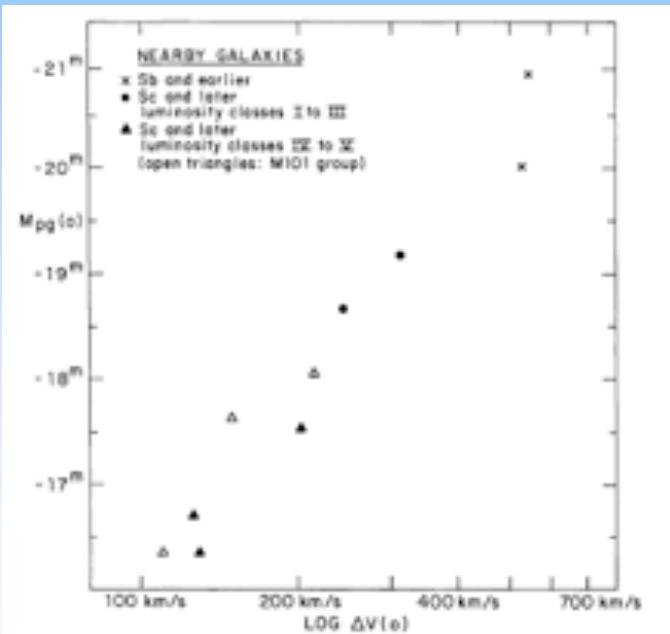
M(DM) increases with M(stars)

Local Galaxies

Fundamental relations for Spirals :

Tully – Fisher relation : brighter Sps have higher max. rotation velocities

Tully & Fisher 77



→ distance / mass determination

rotational velocity ~ M(DM)

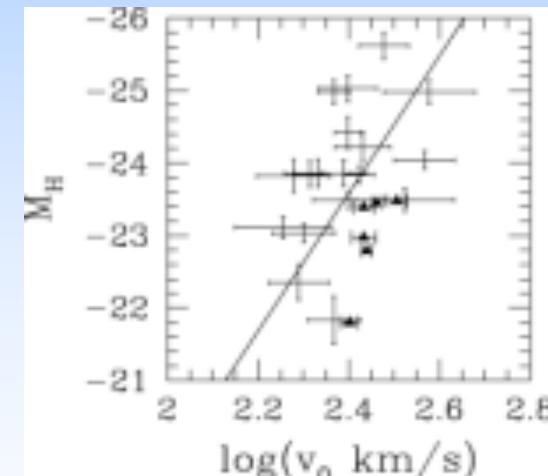
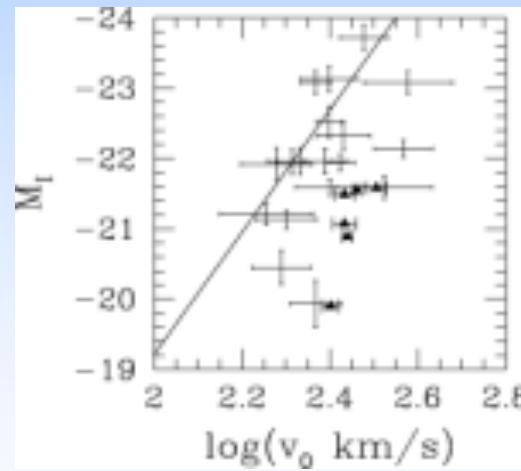


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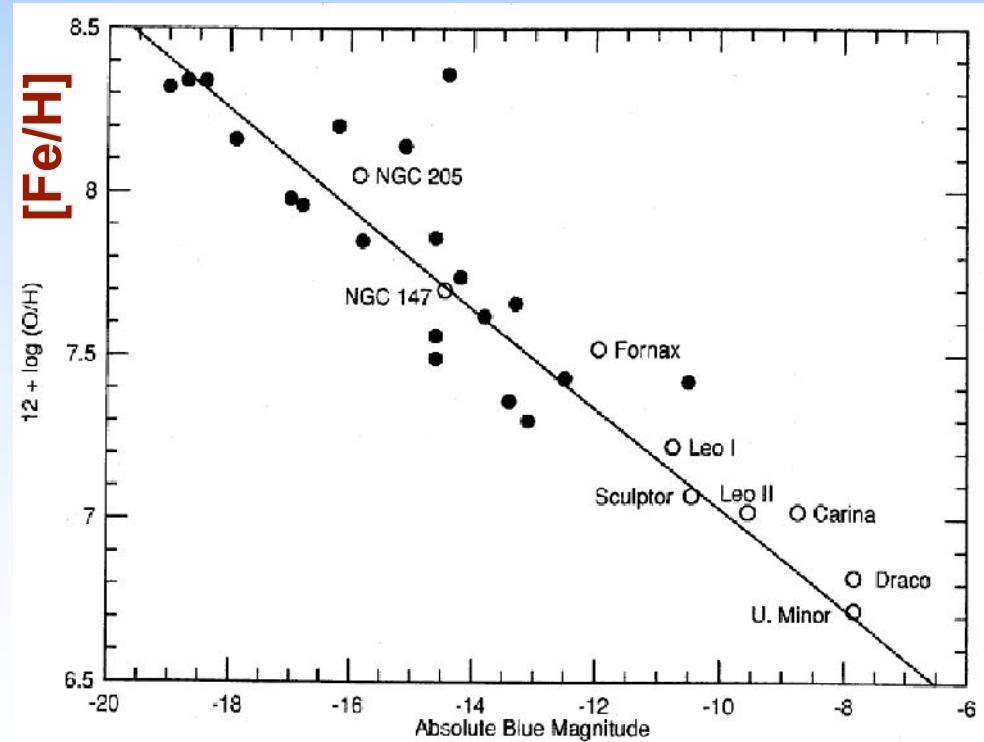
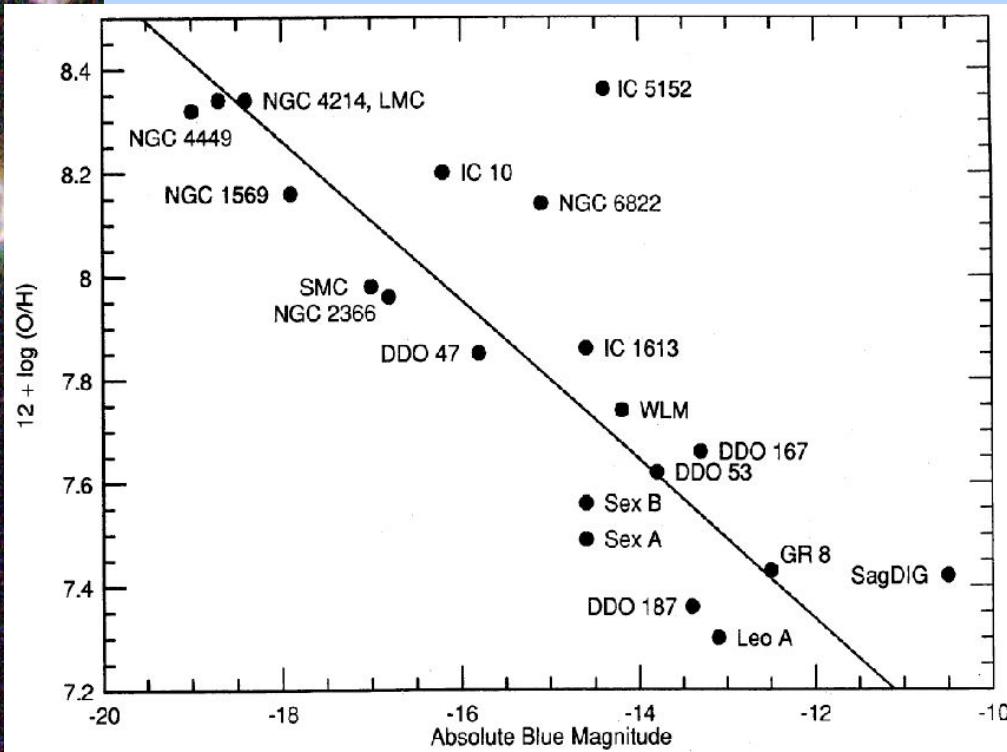
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Local Galaxies

Fundamental relations for Spirals :

Luminosity – metallicity relation : for spirals and Irrs:
brighter Sps/Irrs have higher ISM metallicities
similar to relation for ellipticals (stellar metall.)

(Skillman 89)



Local Galaxies

Luminosity function for galaxies : Schechter 1976

Schechter LF : $\Phi(L) = (\Phi^*/L^*)(L/L^*)^\alpha \exp(-L/L^*)$

L^* : characteristic luminosity

$$M_B^* = -19.7 + 5 \log h$$

Φ^* : (local) normalisation = $1.6 \cdot 10^{-2} h^3 \text{ Mpc}^{-3}$

difficult to determine !

α : faint end slope

$$\phi(L)dL = \phi^* \left(\frac{L}{L^*} \right)^\alpha \exp \left(-\frac{L}{L^*} \right) \frac{dL}{L^*}$$

$$\phi(M)dM = \frac{2}{5} \phi^* (\ln 10) \left[10^{\frac{2}{5}(M^* - M)} \right]^{\alpha+1} \exp \left[-10^{\frac{2}{5}(M^* - M)} \right] dM$$

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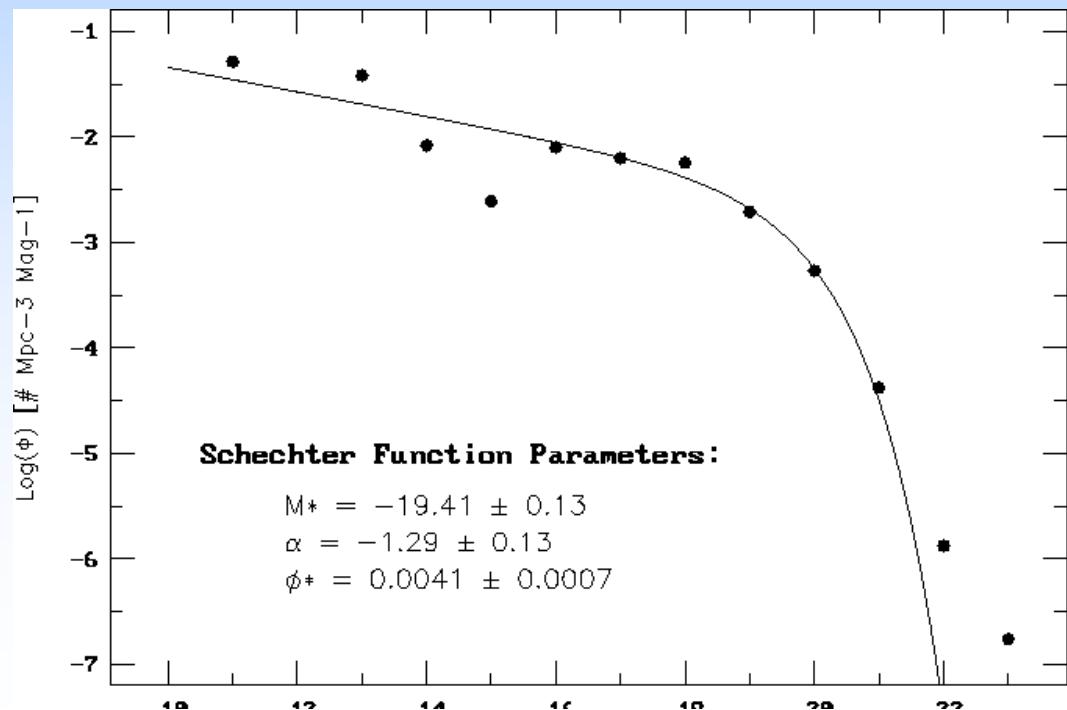
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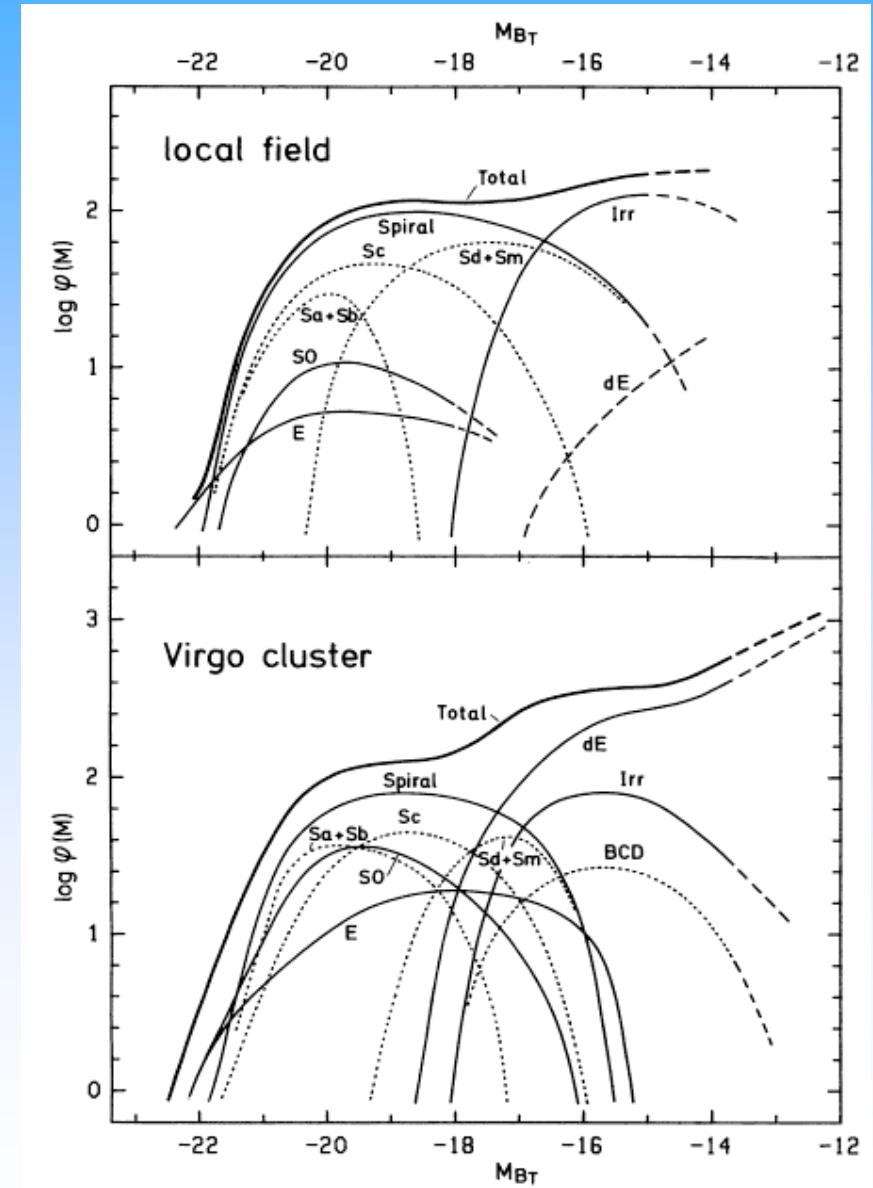
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Local Galaxies

Local luminosity functions for galaxies :
field galaxies
break-down
into types

cluster galaxies:
steep faint end slope





Local Galaxies

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low luminosity galaxies dominate by number

high luminosity galaxies dominate the light

in the local universe

$$M_B^*(E) < M_B^*(Sa) < M_B^*(Sb) < M_B^*(Sc) < M_B^*(Sd)$$

-21.5	-19.7	-18.9	-18.8	-17.7
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with considerable overlap in Virgo (Sandage+85)

Local Galaxies

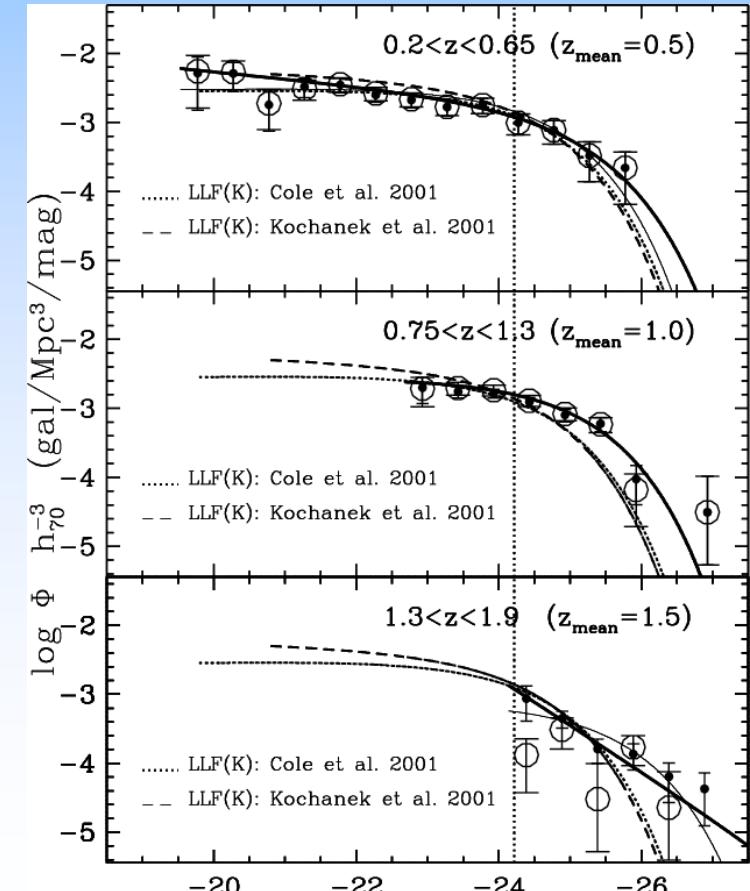
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difficult to determine !

large volume : bright galaxies ok,
faint galaxies incomplete
small volume: faint galaxies
complete,
bright galaxies poor
statistics

redshift evolution :





Local Galaxies

Galaxy mix :

field : normal (=big) galaxies

- >70% Sps
- ~20% Es
- <10% S0s

dwarf-to-normal galaxy number ratio : $\alpha \sim -1.1$

galaxy clusters : >70% S0s

- ~20% Es
- <10% Sps

dwarf -to-normal galaxy number ratio : $\alpha \ll -1.1$

→ transformation of galaxy types



Chemical Evolution : Gas & Stars

Big Bang : H, He, (...., Li)

all heavy elements ($>$ H, He := astrophys. „metals“)

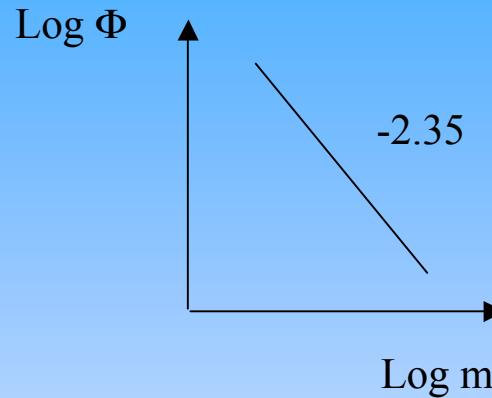
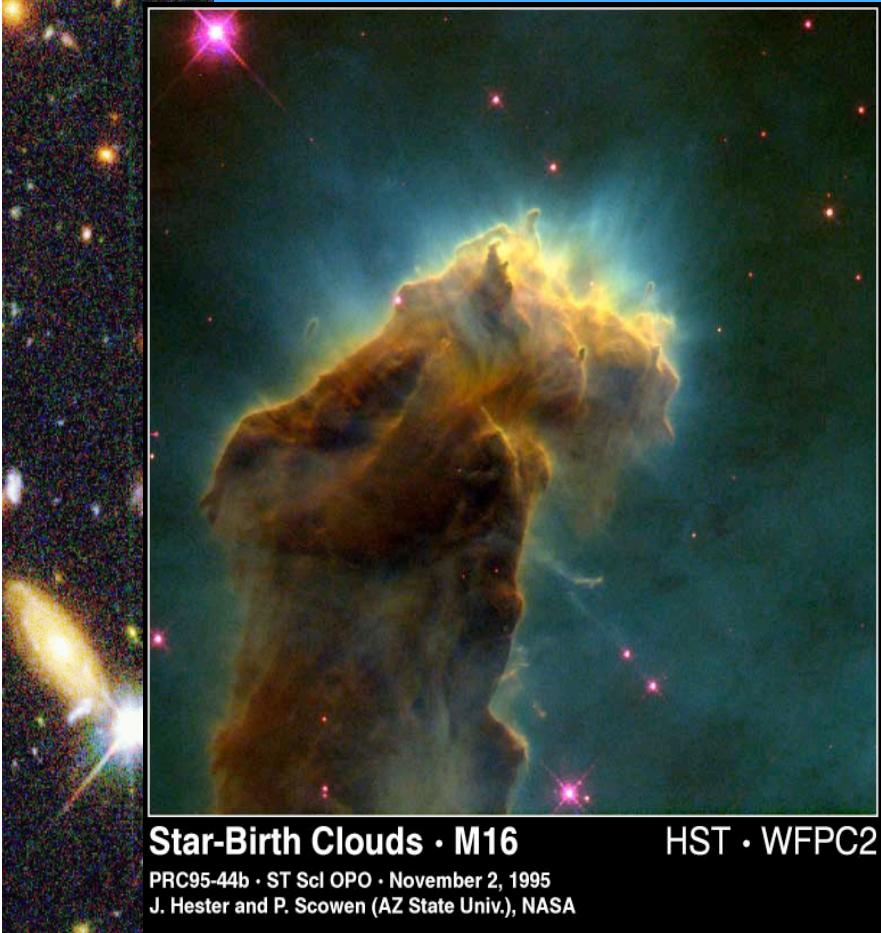
- ↳ fusioned within stars,
- ↳ get back into gas phase through stellar winds, PN, SNe
- ↳ built into later stellar generations

Chemical abundances in the gas determined by

- Stellar Initial Mass Function
- Star Formation History of the galaxy
- Stellar lifetimes & yields (mass, composition)
- In- & outflow of gas
- $Z^{\text{Gas}}(t)$, $X_i^{\text{Gas}}(t)$ from modified Tinsley (68ff) equations
+ SNIa contributions

Chemical & Spectral Evolution of a Galaxy

GALEV



Normalisation :

$$\int_{m_l}^{m_{up}} m \cdot \Phi(m) dm = 1$$

Stellar population :

- **Stellar Initial Mass Function** (Salpeter 1955, Kroupa+ 1993ff)
- **Stellar evolutionary tracks, lifetimes, yields**
- **Star Formation History of the galaxy**